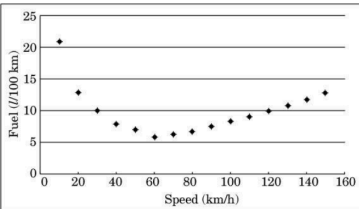



# CBT CLASS XII MATHS AUGUST-2024

## GENERAL INSTRUCTION :

### CHAPTER: CONTINUITY AND DIFFERENTIABILITY & AOD

Sr.No	Question	Marks
	<p><b>Case Study 1</b></p> <p>Let <math>f(x)</math> be a real valued function, then its</p> <p>*Left Hand Derivative (L.H.D.): <math>Lf'(a) = \lim_{(h \rightarrow 0)} \frac{f(a-h) - f(a)}{-h} = (f(a+h) - f(a)) / -h</math></p> <p>*Right Hand Derivative (R.H.D.): <math>Rf'(a) = \lim_{(h \rightarrow 0)} \frac{f(a+h) - f(a)}{h}</math></p> <p>Also, a function <math>f(x)</math> is said to be differentiable at <math>x = a</math>, if L.H.D = R.H.D.</p> <p>If <math>f(x) =  x-3 </math> for <math>x \geq 1</math> and</p> <p><math>f(x) = x^2/4 - 3x/2 + 13/4</math> for <math>x &lt; 1</math></p>	
1	R.H.D. of $f(x)$ at $x = 1$ is (a) 1 (b) -1 (c) 0 (d) 2	1
2	L.H.D. of $f(x)$ at $x = 1$ is (a) -1 (b) 1 (c) 2 (d) 0	1
3	$f(x)$ is not-differentiable at (a) $x = 1$ (b) $x = 2$ (c) $x = 3$ (d) $x = 4$	1
4	Find the value of $f'(2)$ . (a) -1 (b) 1 (c) 2 (d) 0	1
	<p><b>Case Study 2</b></p> <p>Overspeeding increases fuel consumption and decreases fuel economy as a result of tyre rolling friction and air resistance. While vehicles reach optimal fuel economy at different speeds, fuel mileage usually decreases rapidly at speeds above 80 km/h.</p> <div style="display: flex; justify-content: space-around; align-items: center;">   </div> <p>The relation between fuel consumption <math>F</math> (l/100 km) and speed <math>V</math> (km/h) under some constraints is given as <math>F = V^2 / 500 - V/4 + 14</math></p> <p>On the basis of the above information, answer the following questions :</p>	
5	Find $F$ , when $V = 40$ km/h. (a) 7.6 (b) 7.4 (c) 7.3	1

	(d) 7.2	
6	$dF/dV =$ (a) $V - 1/4$ (b) $V/250 - 4$ (c) $V/250 - 1/4$ (d) $2V - 1/4$	1
7	Find the speed $V$ for which fuel consumption $F$ is minimum. (a) 62.5 (b) 63.5 (c) 64.5 (d) 65.5	1
8	Find the quantity of fuel required to travel 600 km at the speed $V$ at which $dF/dV = -0.01$ . (a) 7.2 (b) 6.2 (c) 5.2 (d) 21.2	1
<p><b>Directions: ( Q.9 – Q.10) Each of these questions contains two statements: Assertion (A) and Reason (R). Each of these questions also has four alternative choices, any one of which is the correct answer . You have to select one of the options (a) , (b) , (c) and (d) given below :</b></p> <p><b>(a) A is true , R is true and R is a correct explanation for A</b>  <b>(b) A is true , R is true and R is not a correct explanation for Assertion</b>  <b>(c) A is true and R is false</b>  <b>(d) A is false and R is true</b></p>		
9	<b>Assertion:</b> $ x $ is continuous at $x = 0$ <b>Reason:</b> $f(x)$ is continuous at $x = a$ if $\lim_{x \rightarrow a} f(x) = f(a)$	1
10	Let $f(x) = x^3 - 12x^2 + 36x + 17$ <b>Assertion:</b> $f$ is strictly increasing in $R - (2,6)$ <b>Reason:</b> $f$ is strictly decreasing in $(2,6)$	1

**Answer Key**

<b>Ans1</b>	<b>(b)</b>
<b>Feedback</b>	Option (b) is correct, R.H.D. of $f(x)$ at $x = 1$ is $-1$
<b>Ans2</b>	<b>(a)</b>
<b>Feedback</b>	Option (a) is correct, L.H.D. of $f(x)$ at $x = 1$ is $x = -1$
<b>Ans3</b>	<b>(c)</b>
<b>Feedback</b>	Option (c) is correct, $f(x)$ is not-differentiable at $x = 3$
<b>Ans4</b>	<b>(a)</b>
<b>Feedback</b>	Option (a) is correct, value of $f'(2) = -1$
<b>Ans5</b>	<b>(d)</b>
<b>Feedback</b>	Option (d) is correct, put $V=40$ in $F = V^2 / 500 - V/4 + 14$ so $F = 7.2$
<b>Ans6</b>	<b>(c)</b>
<b>Feedback</b>	Option (c) is correct, $dF/dV = V/250 - 1/4$
<b>Ans7</b>	<b>(a)</b>
<b>Feedback</b>	Option (a) is correct, $dF/dV = V/250 - 1/4 = 0$ and $V = 62.5$ km/h
<b>Ans8</b>	<b>(b)</b>
<b>Feedback</b>	Option (b) is correct, $dF/dV = V/250 - 1/4 = -0.01$ and by solving $V = 60$ km /h and required $F = 3600/500 - 15 + 14 = 6.2$
<b>Ans9</b>	<b>(a)</b>
<b>Feedback</b>	Option (a) is correct, A is true , R is true and R is a correct explanation for A
<b>Ans10</b>	<b>(b)</b>
<b>Feedback</b>	Option (b) is correct, A is true , R is true and R is not a correct explanation for A